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# Strangeness spin in the proton studied with neutrino scattering

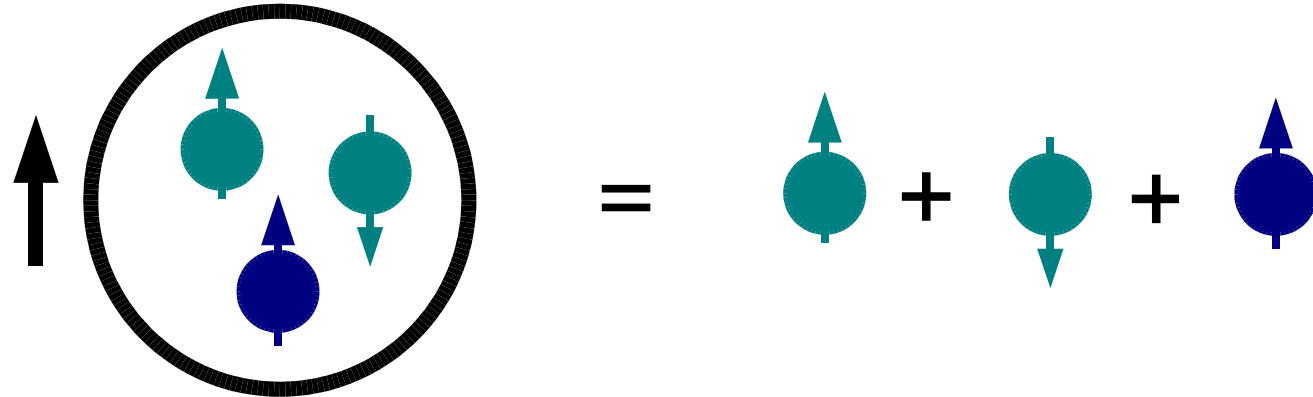
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# Spin structure of nucleon

Nucleon spin:  $\frac{1}{2}$  = sum of quarks spin



$$\frac{1}{2} = \frac{1}{2} \Delta \Sigma = \frac{1}{2} (\Delta u + \Delta d + \Delta s + \Delta \bar{u} + \Delta \bar{d} + \Delta \bar{s}) \quad \Delta q = q^\uparrow - q^\downarrow$$

The most naive case:  $\Delta \Sigma = \Delta u + \Delta d + \Delta s = 1$

Naive Parton model:

Assuming SU(3) flavor symmetry, taking axial current

$$\Delta \Sigma = \Delta u + \Delta d + \Delta s = a_0$$

$$\Delta u - \Delta d = a_3$$

$$\Delta u + \Delta d - 2\Delta s = a_8$$

From weak decay:

$$a_3 = 1.26,$$

$$a_8 = 0.58$$

if  $\Delta s = 0$ ,  $\Delta \Sigma = a_8 = 0.58$

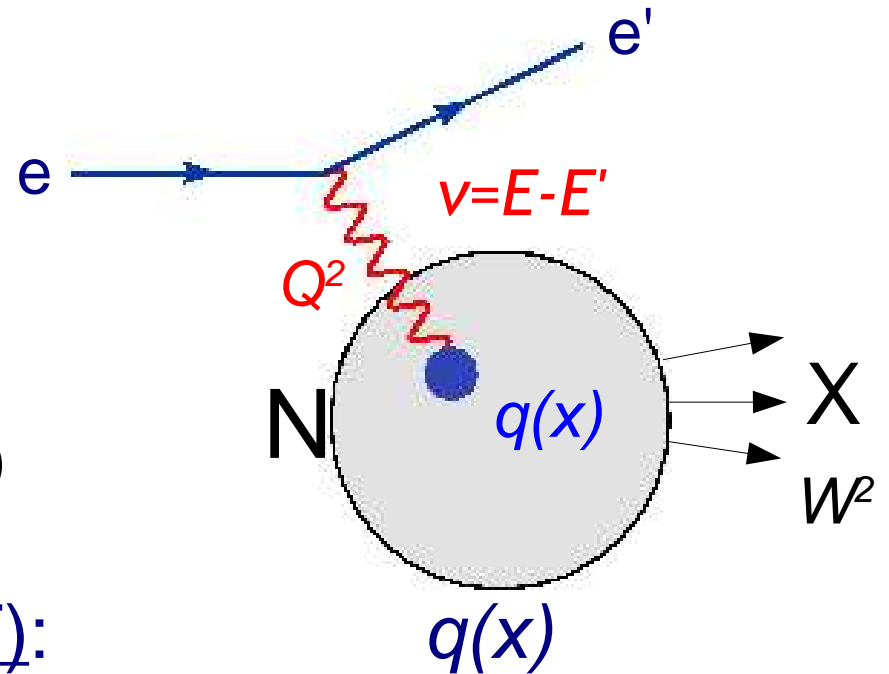
# Deep Inelastic Scattering and PDF

## Deep Inelastic Scattering (DIS):

$$e + N \rightarrow e' + X$$

$$Q^2 > 1 \text{ GeV}^2, W^2 > 10 \text{ GeV}^2$$

$$= \sum_q (e\text{-}q \text{ elastic scattering})$$



## Parton Distribution Function (PDF):

Probability distribution of finding quark inside nucleon which carries momentum fraction  $x = Q^2 / 2Mv$ .

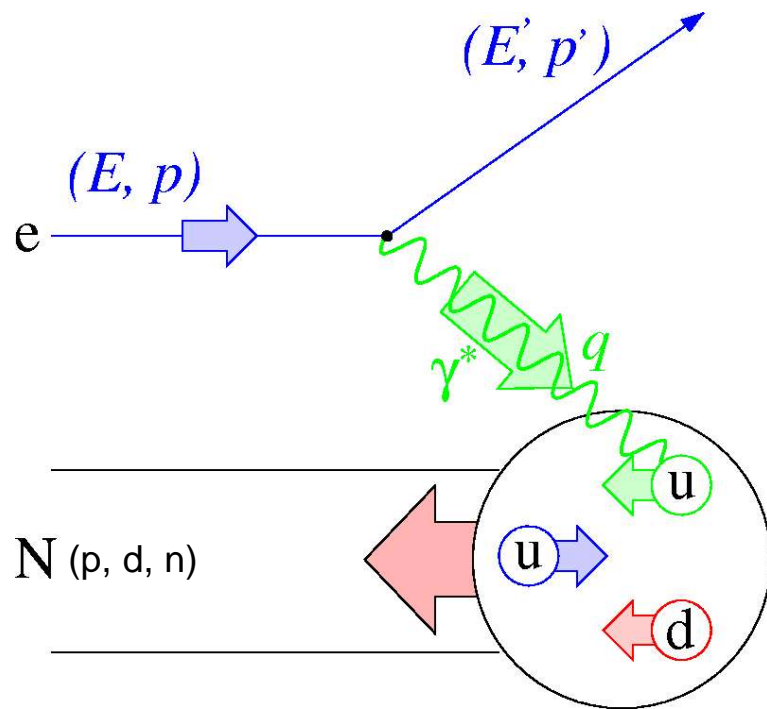
$$\frac{d^2 \sigma}{dx dy} = \frac{2\pi \alpha^2 s}{Q^4} (x y^2 F_1(x) + (1-y) F_2(x))$$

$$F_1(x) = \frac{1}{2} \sum_q e_q^2 q(x)$$

$$F_2(x) = 2x F_1(x)$$

# Polarized DIS measurement

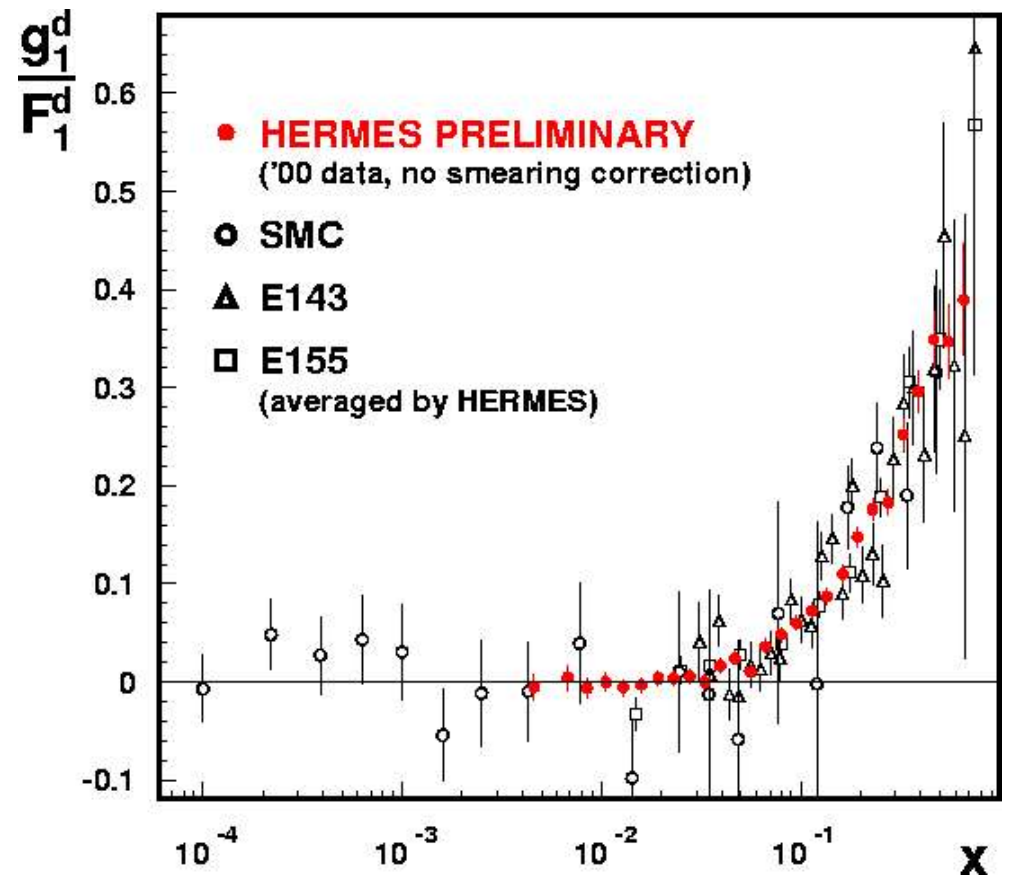
$$\vec{l} + \vec{N} \rightarrow l' + X$$



$$g_1(x) = \frac{1}{2} \sum_q e_q^2 \Delta q(x)$$

$$\Delta q(x) = q^\uparrow(x) - q^\downarrow(x)$$

$$A_1 = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}} = \frac{g_1}{F_1} = \frac{\sum_q e_q^2 \Delta q(x)}{\sum_q e_q^2 q(x)}$$



# Quark spin contribution

EMC finding:

“Spin Puzzle” (Nucl. Phys. B328 (1989) 1)

$$\int_0^1 dx g_1^p(x) = \frac{1}{9} a_0 + \frac{1}{12} a_3 + \frac{1}{36} a_8 = 0.126 \pm 0.01 \pm 0.015$$

From weak decay:  $a_3 = 1.26$ ,  $a_8 = 0.58$

assuming flavor SU(3)

$$a_0 \sim 0.1$$

$$\rightarrow \Delta \Sigma = 0.1, \quad \Delta s + \Delta \bar{s} \sim -0.19$$

$$\rightarrow \text{axial anomaly: } a_0 = \Delta \Sigma - 3 \frac{\alpha_s}{2\pi} \Delta G \quad \Delta G > 0$$

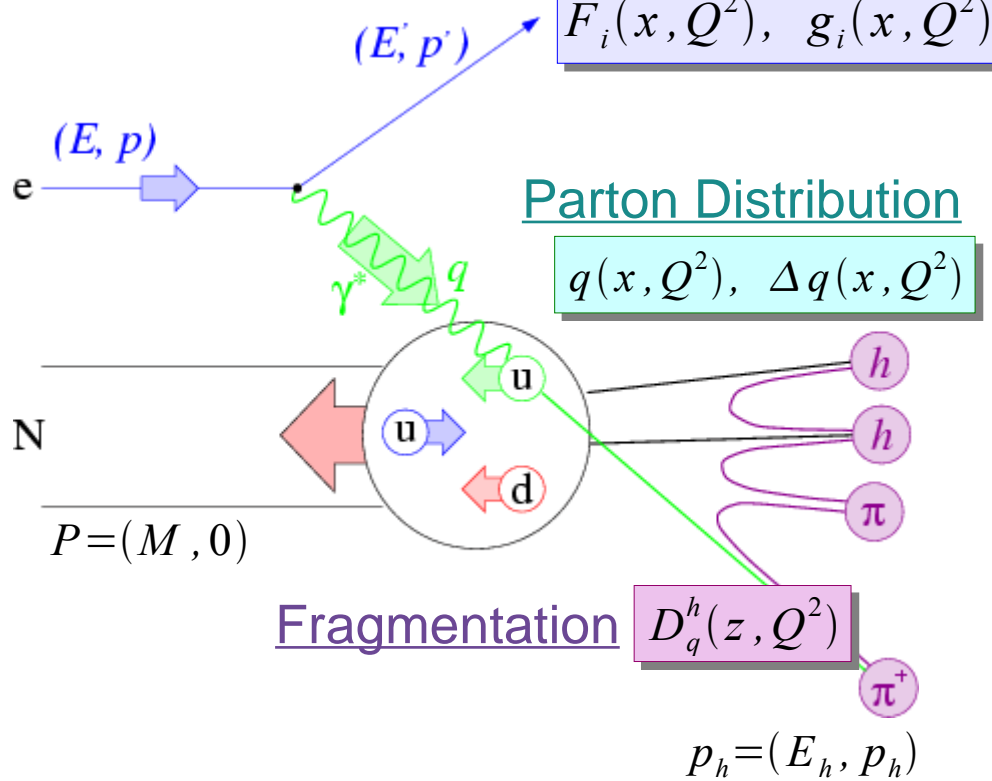
# Hadron coincidence measurement

## Semi-inclusive measurement of DIS

$$\vec{l} + \vec{N} \rightarrow l' + h + X$$

Structure Function

$$F_i(x, Q^2), g_i(x, Q^2)$$



Measure hadron(s) in coincidence with the scattered lepton

$$\frac{d^3 \Delta \sigma^h}{dx dz dQ^2} \propto \sum_i e_q^2 \Delta q(x, Q^2) D_q^h(z, Q^2)$$

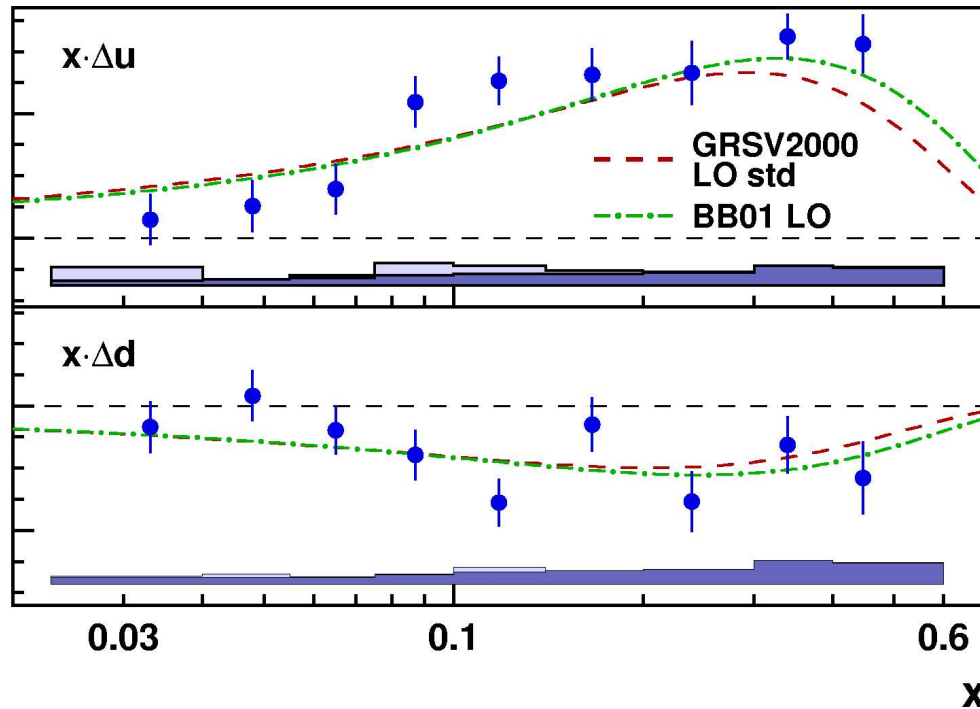
$$z = \frac{P \cdot p_h}{P \cdot q} = \frac{E_h}{\nu}$$

### Flavor Tagging:

Hadron carries information on quark flavor through fragmentation function

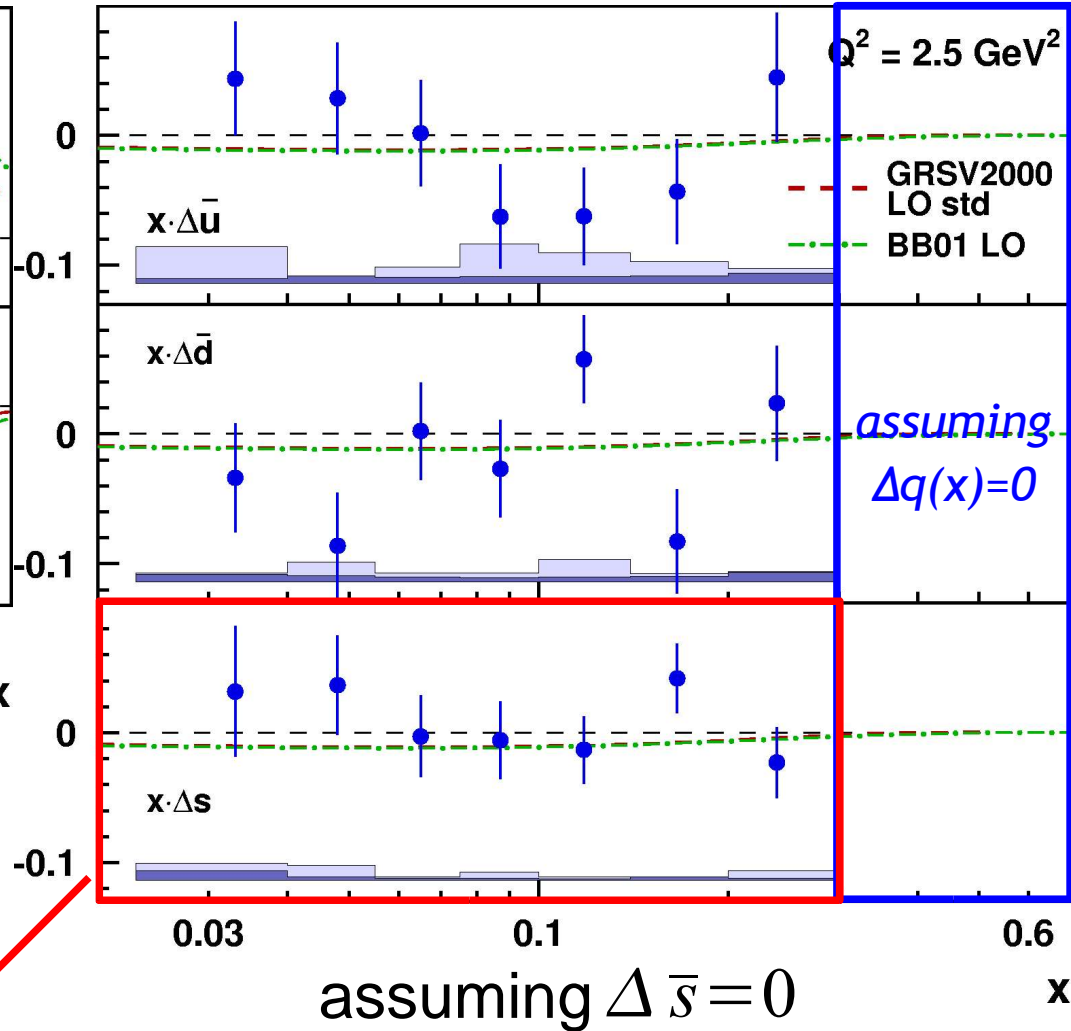
# Results from HERMES

$$Q^2 = 2.5 \text{ GeV}^2$$



$$\Delta q = \int_{0.023}^{0.6} dx \Delta q(x) \quad Q^2 = 2.5 \text{ GeV}^2$$

$$\begin{aligned} \Delta u &= 0.601 \pm 0.039 \pm 0.049 \\ \Delta d &= -.226 \pm 0.039 \pm 0.050 \\ \Delta \bar{u} &= -.002 \pm 0.036 \pm 0.023 \\ \Delta \bar{d} &= -.054 \pm 0.033 \pm 0.011 \\ \Delta s &= 0.028 \pm 0.033 \pm 0.009 \end{aligned}$$



Free from SU(3) flavor symmetry assumption



# Neutrino-Nucleon scattering

$$\frac{d\sigma}{dQ^2} = \frac{G_F^2}{2\pi} \frac{Q^2}{E_\nu^2} \left( A \pm BW \pm CW^2 \right)$$

$$W = \frac{4E_\nu}{m_p} - \frac{Q^2}{m_p^2}$$

$$A = \frac{1}{4} \left[ G_1^2 (1 + \tau) - (F_1^2 - \tau F_2^2) (1 - \tau) + 4\tau F_1 F_2 \right]$$

$$\tau = \frac{Q^2}{4m_p^2}$$

$$B = -\frac{1}{4} G_1 (F_1 + F_2)$$

$$C = \frac{1}{16} \frac{m_p^2}{Q^2} (G_1^2 + F_1^2 + \tau F_2^2)$$

NC-EL/CC-QE

Neutral Current

$$F_{1,2} = \left[ \left[ \frac{1}{2} - \sin^2 \theta_W \right] [F_{1,2}^p - F_{1,2}^n] - \sin^2 \theta_W [F_{1,2}^p + F_{1,2}^n] - \frac{1}{2} F_{1,2}^s \right]$$

$$G_1 = \left[ -\frac{G_A}{2} \tau_z + \frac{G_A^s}{2} \right]$$

$$G_A^s(Q^2=0) = \Delta s$$

$\tau_z = 1$  for proton,  $-1$  for neutron

# Neutrino scattering and $\Delta s$

- Neutral current cross section  $\rightarrow$  strange axial form factor
- From  $G_A^s(Q^2)$  to  $\Delta s$

$$G_A^s(Q^2 \rightarrow 0) = \Delta s = -0.21 \pm 0.10$$

Further analysis: (Alberico *et al.*)

$$R_{NC/CC}^\nu = 0.152 \pm 0.007 \pm 0.017$$

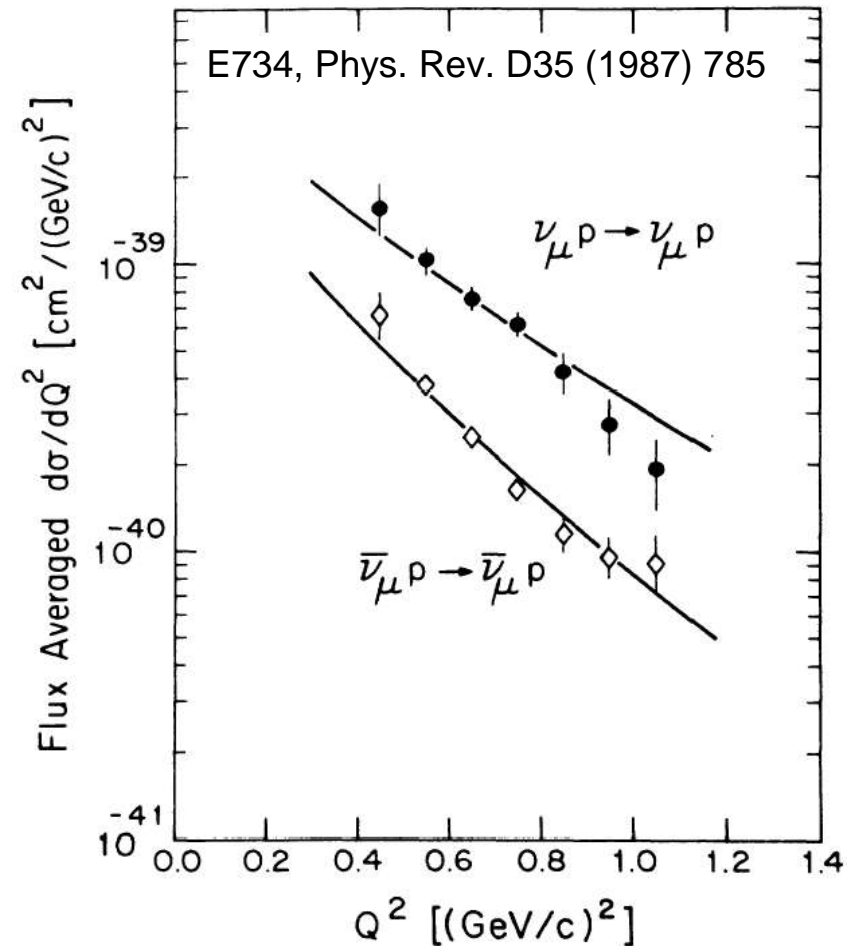
$$R_{NC/CC}^{\bar{\nu}} = 0.218 \pm 0.012 \pm 0.023$$

$$R_{NC}^{\nu/\bar{\nu}} = 0.302 \pm 0.019 \pm 0.037$$

$0.5 < Q^2 < 1.0 \text{ GeV}^2$

$$-0.21 < \Delta s < 0$$

strong correlation with the axial mass  $M_A$



# Strangeness spin in nucleon

$\phi$  production in  $p\bar{p}$  annihilation: polarized strangeness

DIS inclusive measurement:  $\Delta s = \int_0^1 ds(x) dx = -0.13 \pm 0.06$   
required SU(3) flavor symmetry and several assumptions

DIS semi-inclusive measurement:  $\Delta s = \int_{0.023}^{0.6} ds(x) dx = 0.03 \pm 0.03$   
Unknown contribution from the low x region (same in inclusive measurement)

Neutrino scattering:  $-0.2 < \Delta s < 0$   
global strange form factors analysis resulted in the positive solution, too.  
(with parity violating electron scattering data)

Baryon magnetic moment:  $\Delta s \sim -0.2$

Lattice calculation:  $\Delta s \sim -0.1$

Precise determination  $\delta(\Delta s) < 0.04$  is important.

# Using superbeams

## Axial Form Factor Measurement

# Methods to extract $\Delta s$

NC cross section:

$$\sigma^{NC}(Q^2) \rightarrow G_A^s(Q^2) \xrightarrow{Q^2 \rightarrow 0} G_A^s(0)$$

NC cross section p/n ratio:

$$R_{p/n}^v(Q^2) = \frac{(d\sigma/dQ^2)_{(v,p)}^{NC}}{(d\sigma/dQ^2)_{(v,n)}^{NC}}$$

NC/CC asymmetry:

$$A(Q^2) = \frac{(d\sigma/dQ^2)_v^{NC} - (d\sigma/dQ^2)_{\bar{v}}^{NC}}{(d\sigma/dQ^2)_v^{CC} - (d\sigma/dQ^2)_{\bar{v}}^{CC}}$$

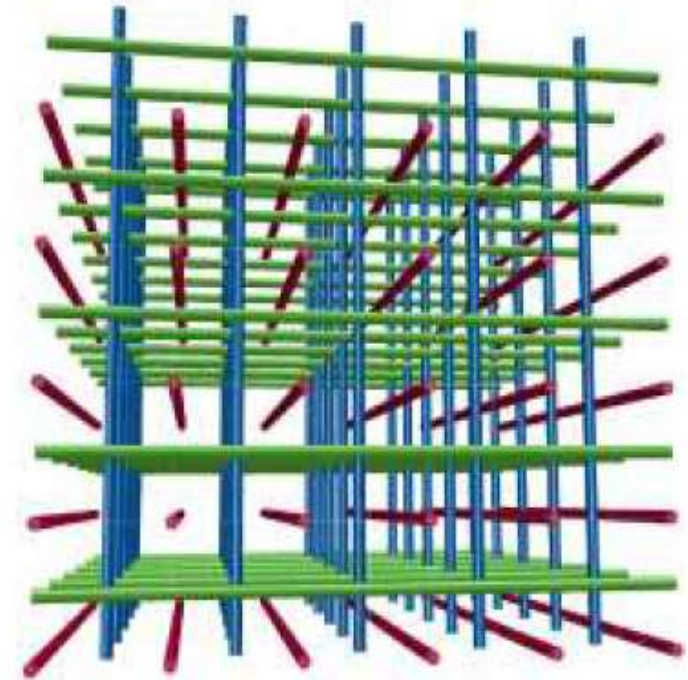
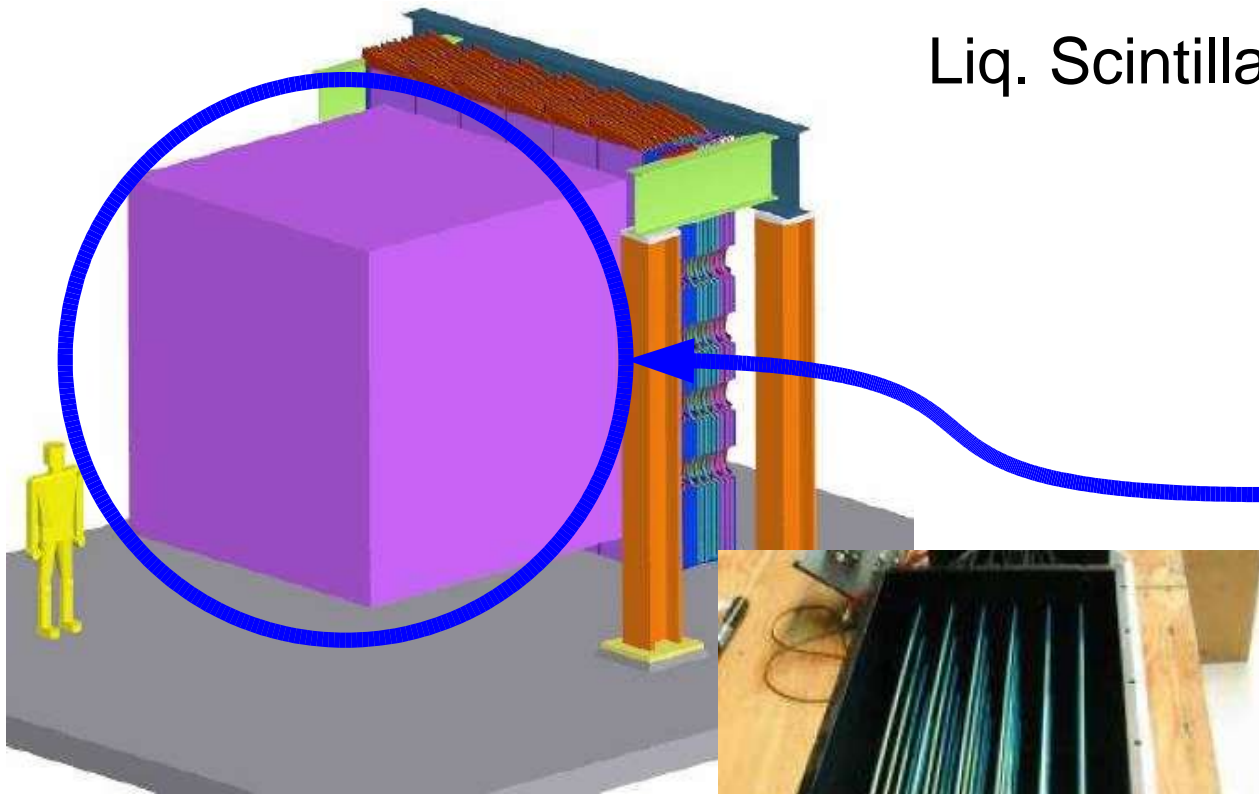
NC/CC ratio:

$$R_{NC/CC}(Q^2) = \frac{(d\sigma/dQ^2)_v^{NC}}{(d\sigma/dQ^2)_v^{CC}}$$

# FINeSSE

## Fermilab Intense Neutrino Scattering Scintillator Experiment

Liq. Scintillator readout with WS fibers

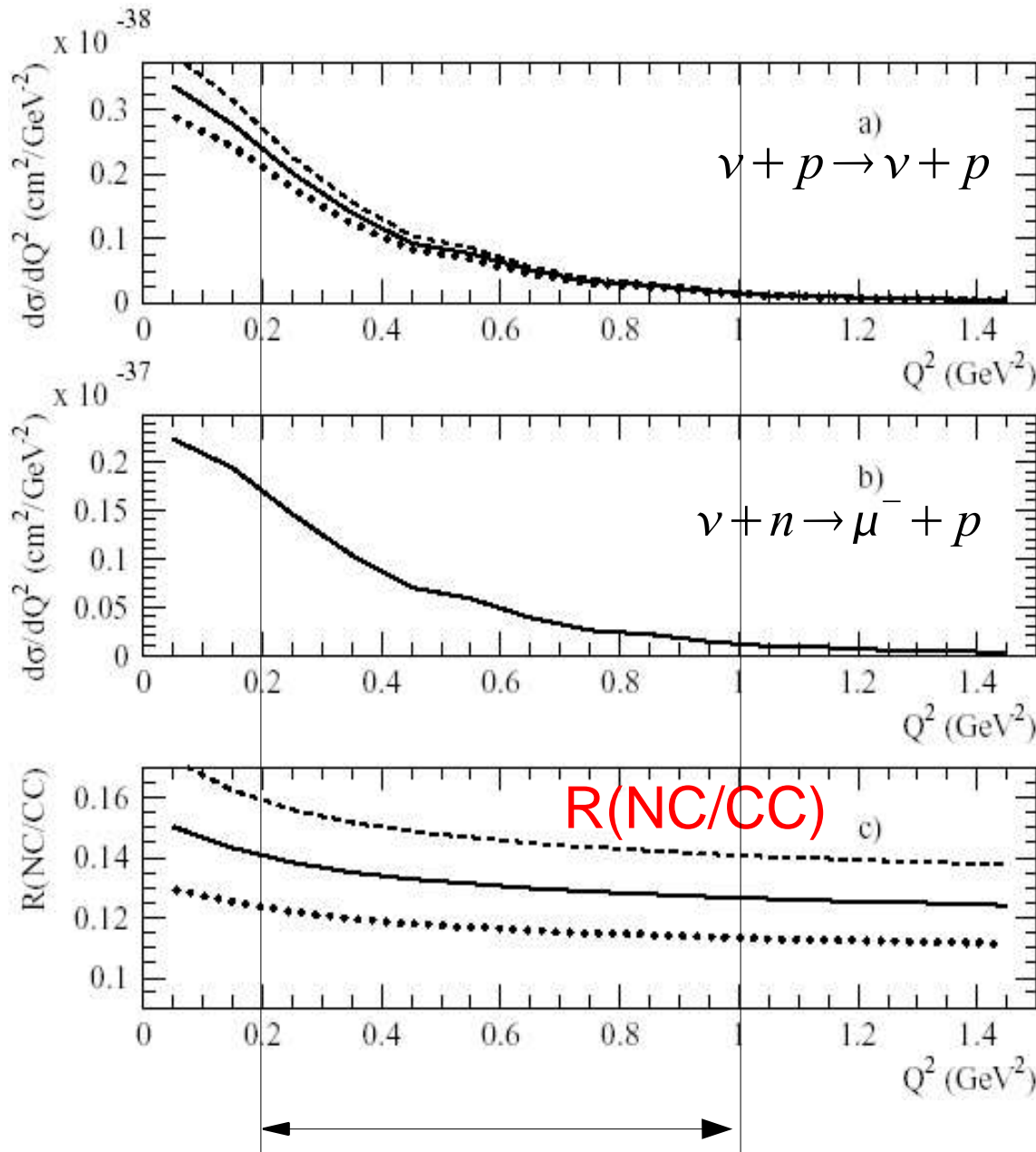


FINeSSE detector  
Prototype

Proposal: Fermilab  
LOI: BNL

# R(NC/CC) measurement -FINeSSE-

Monte Carlo Estimation



target: C in Liq. Scinti.

R(NC/CC) cancels:  
flux  
nuclear effects

$$G_A^S = -0.1$$

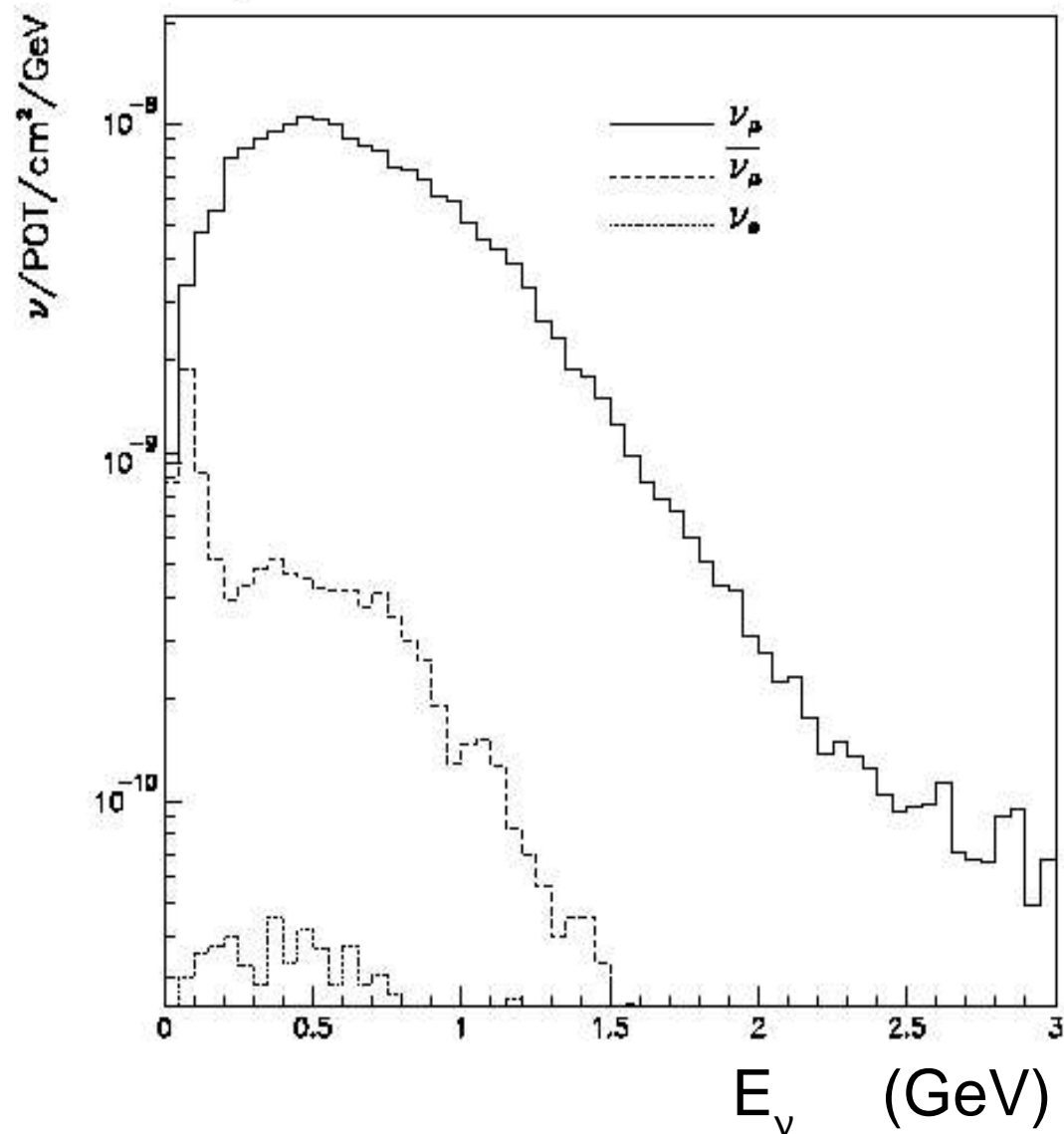
$$G_A^S = 0$$

$$G_A^S = 0.1$$

from FINeSSE LOI

# FINeSSE at Fermilab hep-ex/0402007

Expected Fluxes at 100m with 25m absorber



Fermilab Booster  
used for MiniBooNE

6E+20 POT in 2 years

R(NC/CC) measurement:

FINeSSE

$0.2 < Q^2 < 1.0$

stat. error: 2%

sys. error: 5%

E734

$0.5 < Q^2 < 1.0$

5%

11%



$$\delta(\Delta s) < 0.04$$



# What should be considered?

- **Nuclear Effects**

- Target: Carbon in the liquid scintillator.
- Is it canceled in the ratio  $R(\text{NC}/\text{CC})$  over the entire  $Q^2$  range?

- **$Q^2$  extrapolation**

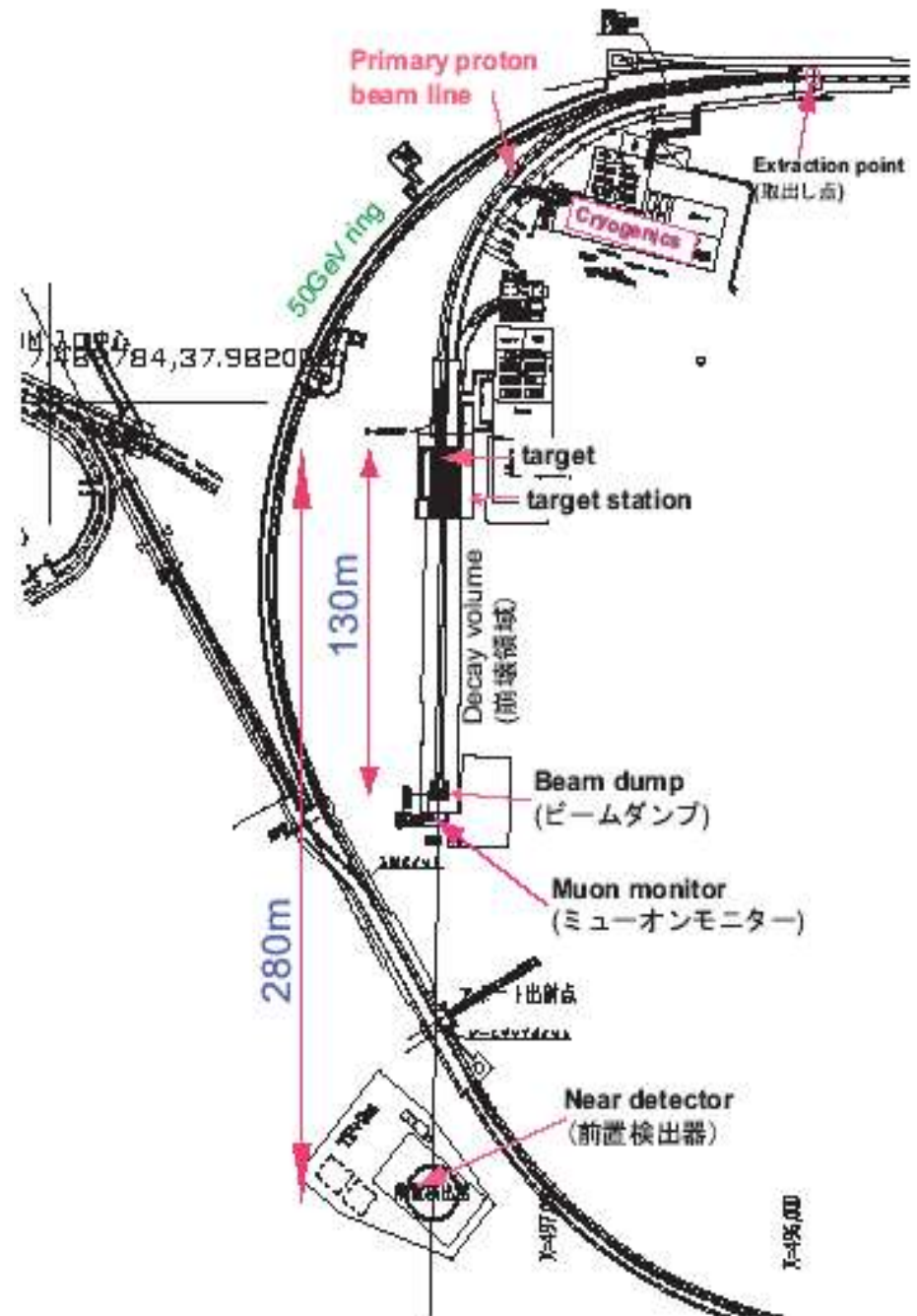
- rely on the dipole form factor.
  - uncertainty below  $Q^2=0.2 \text{ GeV}^2$
- Nuclear effects in the very low  $Q^2$  region

**J-PARC**

# J-PARC $\nu$ -beam line

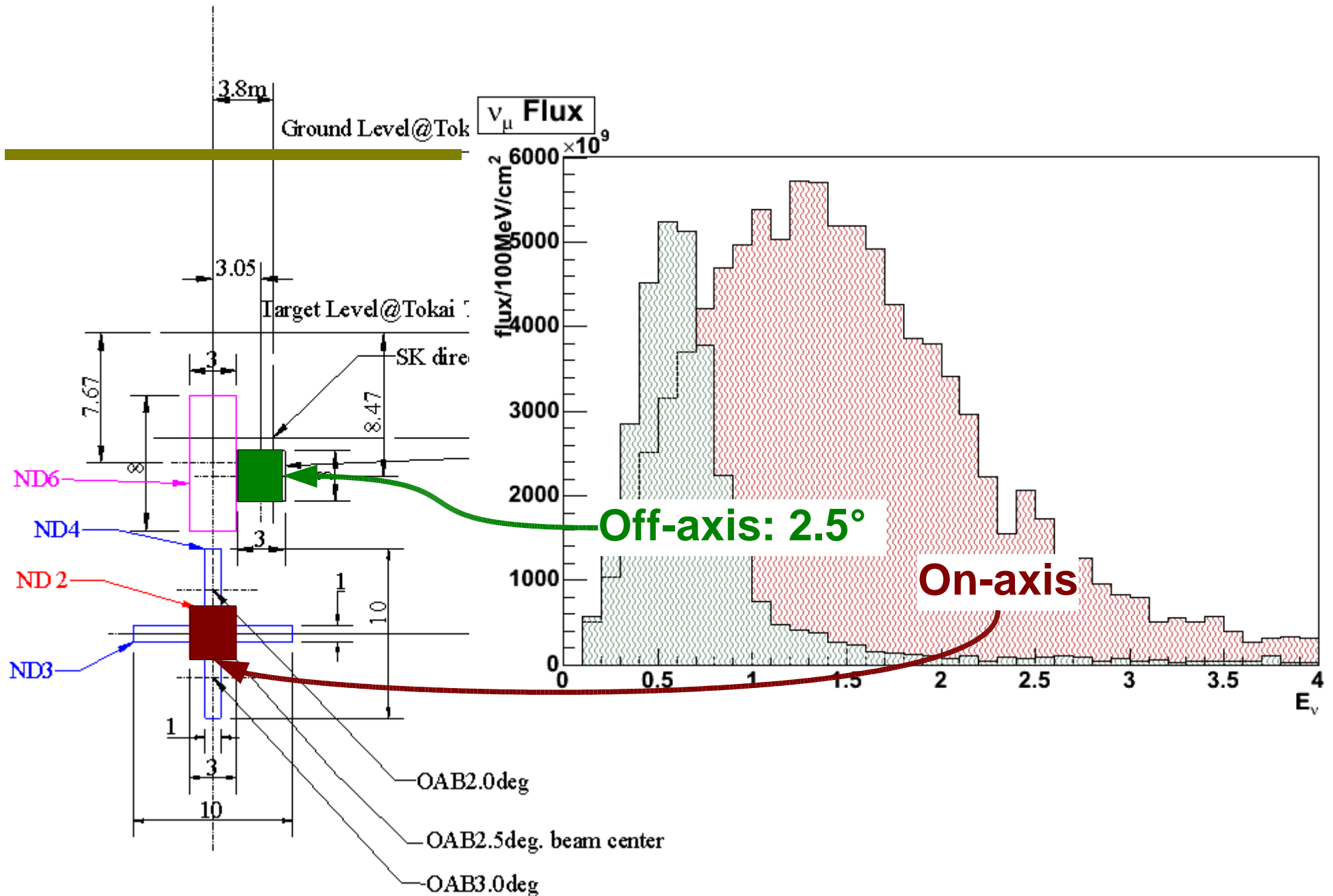
- **Neutrino beam**
  - peak around 1 GeV for “on-axis”, 0.8 GeV for “off-axis”
  - $10^{21}$  POT/year
  - with anti-neutrino beam

- neutrino anti-neutrino asymmetry measurement



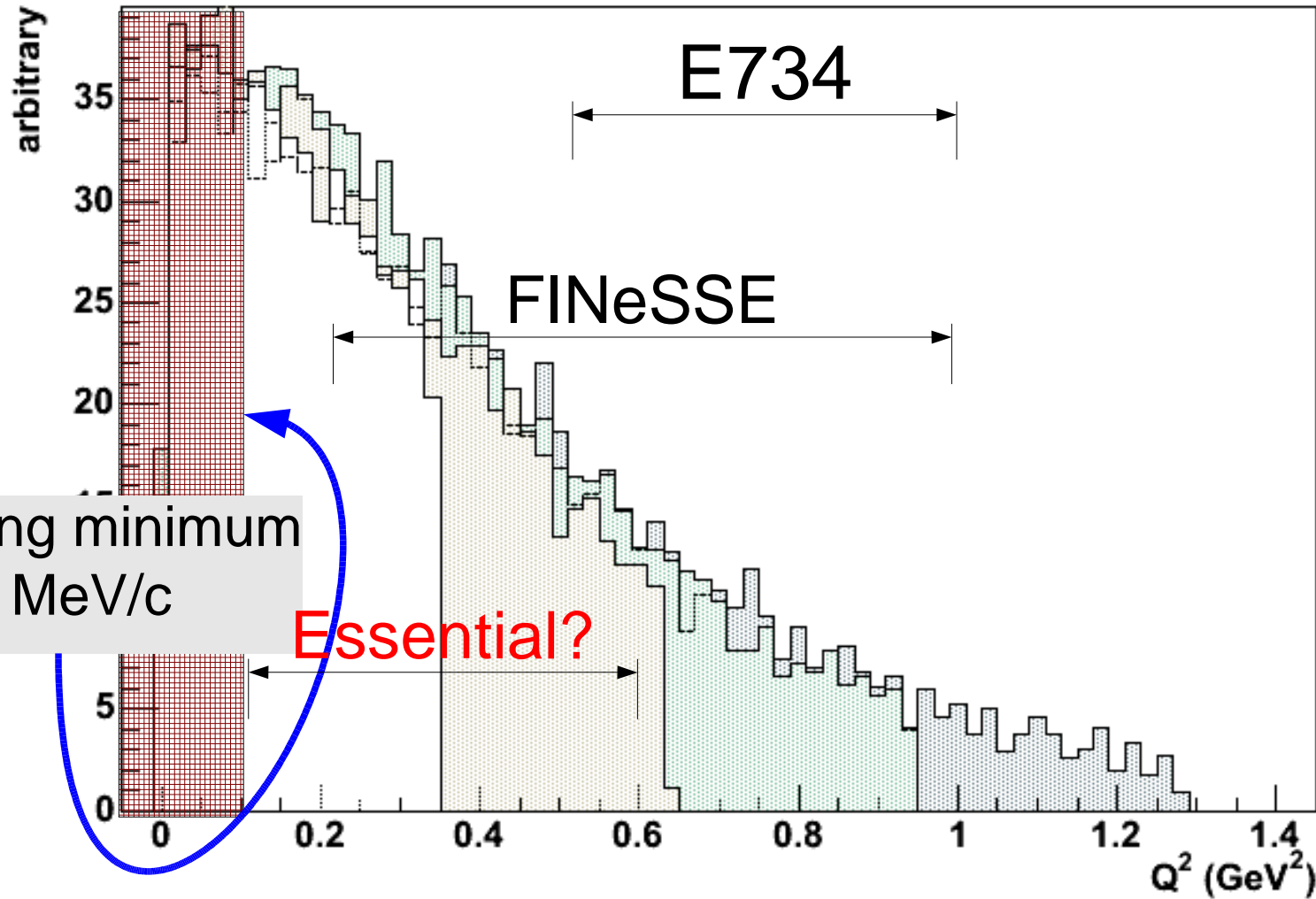
# Neutrino Flux

(Neutrino Flux Monte Carlo Data)



# Neutral current elastic scattering

NC-EL  $Q^2$  Distribution



assuming minimum  
 $T_p = 40$  MeV/c

Essential?

$E_\nu = 0.4 \quad 0.6 \quad 0.8 \quad 1.0$  GeV

monochromatic energy

# What can we do?

- **Elastic scattering measurement**

- NC, CCQE:  $\sigma$  or R(NC/CC) measurement
- Neutrino anti-neutrino asymmetry measurement
- background control: neutral  $\pi$  production, neutron

- **Nuclear effects**

- Use different mixture of H/C? Liquid Scintillator?
- Hydrogen target if possible. Hydrogen TPC?

- **$Q^2$  extrapolation**

- $G_a^s$  at  $Q^2=0$  gives  $\Delta s$ : need to extrapolate  $Q^2=0$
- as low  $Q^2$  as possible: precise reconstruction of recoil proton

# Summary

- **Strangeness spin in the nucleon**
  - has been studied with various probes
  - statistical and systematic uncertainties
- **Neutrino scattering**
  - Unique tool for studying strangeness spin: nucleon axial form factor measurement
  - Key points: nuclear effects,  $Q^2$  extrapolation
  - Measurement at J-PARC: studies are on going.